

## DEPARTMENT OF MATHEMATICS

### B. Sc. Mathematics

#### PROGRAM SPECIFIC OUTCOMES

After the successful completion of this course, the student will: -

- Be able to explain the core ideas and the techniques of mathematics at the college level.
- Understand the applications of Mathematics in other disciplines and basic concepts and tools of mathematical logic, set theory, methods of proof, geometry, calculus, abstract structures and analysis.
- Be able to setup mathematical models of real world problems and obtain solutions in structured and analytical approaches with independent judgement.
- Be able to carry out objective analysis and prediction of quantitative information with independent judgment.
- Be able to communicate effectively about mathematics to both lay and expert audiences utilizing appropriate information and communication technology.
- Develop logical, computational and typesetting skills and implement them practically.
- Be able to recognize the importance of compliance with the ethics of science and being a responsible citizen towards their community and a sustainable environment.
- Be able to cultivate a mathematical attitude and nurture the interests.

#### COURSE OUTCOMES

##### **FIRST SEMESTER MM1CRT01: FOUNDATION OF MATHEMATICS**

On completion of this course, successful students will be able to:

- prove statements about sets and functions;
- Develop knowledge in basic concepts of Mathematics.
- Construct simple proofs
- Understand the concepts of mathematical logic, sets, functions, relations and partial orderings.
  - Apply proof techniques to prove simple theorems.
  - Determine the solution of polynomial equation upto 4th degree.

##### **SECOND SEMESTER MM2CRT02: ANALYTIC GEOMETRY, TRIGONOMETRY AND DIFFERENTIAL CALCULUS**

On completion of this course, successful students will be able to:

- find the equation to tangent, normal at a point on a conic;
- find the polar equation of a line, circle, tangent and normal to conics
- familiarize real and imaginary parts of a circular and hyperbolic functions of a complex variable
- Factorization of special type of polynomial functions
- Find the higher order derivative of the product of two functions
- familiarize indeterminate forms

### **THIRD SEMESTER MM3CRT03: CALCULUS**

- After completing this course the learner should be able to
- Expand a function using Taylor's and Maclaurin's series.
- Conceive the concept of asymptotes and obtain their equations.
- Understand curvature, involutes, evolutes, envelopes
- Learn about partial derivatives and its applications.
- Find the area under a given curve, length of an arc of a curve when the equations are given in parametric and polar form.
- Find the area and volume by applying the techniques of double and triple integrals

### **FOURTH SEMESTER**

#### **MM2CRT04: VECTOR CALCULUS, THEORY OF NUMBERS AND LAPLACE TRANSFORM**

After completing this course the learner should be able to

- Analyze vector functions to find derivatives, tangent lines, integrals, arc length, and curvature,
- Compute limits and directional derivatives of functions of 2 and 3 variables,
- Differentiate vector fields
- Determine gradient vector fields and find potential functions
- Analyse the fundamental theorem of calculus and see their relation to the fundamental theorems of calculus in calculus, leading to the more generalised version of Stokes' theorem in the setting of differential forms.
- Understand basic properties of congruence,
- familiarize famous theorems - Fermat's Theorem, Wilson's Theorem
- Understand the properties of Euler –Phi Function
- Develop the idea about Laplace Transform and its properties
- Solve linear differential equations using the Laplace transform technique,

### **FIFTH SEMESTER**

#### **MM5CRT05: MATHEMATICAL ANALYSIS**

After completing this course the learner should be able to

- Describe the real line as a complete, ordered field
- Determine the basic algebraic and order properties of real numbers
- Understand the term convergence
- Use the definitions of convergence as they apply to sequences, series and functions,
- Produce rigorous proofs of results that arise in the context of real analysis.
- Write solutions to problems and proofs of theorems that meet rigorous standards based on content, organization and coherence, argument and support, and style

#### **MM5CRT06: DIFFERENTIAL EQUATIONS**

- After studying this course the students should be able to
  - Obtain an integrating factor which may reduce a given differential equation into an exact one and eventually provide its solution.
  - Identify and obtain the solution of Clairaut's equation.
  - Find the complementary function and particular integrals of linear differential equation.
  - Familiarize the orthogonal trajectory of the system of curves on a given surface.
  - Describe the origin of partial differential equation and distinguish the integrals of first order linear partial differential equation into complete, general and singular integrals.
  - Use Lagrange's method for solving the first order linear partial differential equation
  - Solve differential equations of first order using graphical, numerical, and analytical methods,
  - Solve and apply linear differential equations of second order (and higher),
  - Find power series solutions of differential equations, and
  - Develop the ability to apply differential equations to significant applied and/or theoretical problems.
  - Demonstrate their ability to write coherent mathematical proofs and scientific arguments needed to communicate the results obtained from differential equation models
  - Demonstrate their understanding of how physical phenomena are modeled by differential equations and dynamical systems
  - Implement solution methods using appropriate technology.

#### **MM5CRT07: ABSTRACT ALGEBRA**

After completing this course the learner should be able to

- Assess properties implied by the definitions of groups and rings,
- Use various canonical types of groups (including cyclic groups and groups of permutations) and canonical types of rings (including polynomial rings and modular rings),
- Analyze and demonstrate examples of subgroups, normal subgroups and quotient groups,
- Analyze and demonstrate examples of ideals and quotient rings,
- Use the concepts of isomorphism and homomorphism for groups and rings
- Produce rigorous proofs of propositions arising in the context of abstract algebra

#### **CODE: HUMAN RIGHTS AND MATHEMATICS FOR ENVIRONMENTAL STUDIES**

After the completion of this course the student will be able to:

- Help the students to understand how their decisions and actions affect the environment.
- Build knowledge and skills necessary to address complex environmental issues ,and ways we can take action to keep our environment healthy and sustainable for future
- Help the students to understand basic concepts of Human Rights

- Understand about Fundamental Rights and Indian Constitution
- Identify the Application of Mathematics in Nature
- Develop the idea about the Fibonacci numbers and Golden ratio in nature

Open course

### **MM5GET02: APPLICABLE MATHEMATICS**

- After the completion of this course the student will be able to
  - Understanding the basic operations of Mathematics
  - Applies shortcut methods for solving problems
  - Apply mathematical concepts and principles to perform computations
  - Apply mathematics to solve real life problems
  - Create, use and analyze graphical representations of mathematical relationships
  - Communicate mathematical knowledge and understanding
  - Apply technology tools to solve problems · Perform abstract mathematical reasoning
  - Learn independently
  - Compute limits, derivatives, and definite & indefinite integrals of algebraic, logarithmic and exponential functions
  - Analyze functions and their graphs as informed by limits and derivatives
  - Familiarize with basic operations on real numbers, logarithms and quadratic equations
  - Identify the definitions of trigonometric ratios and their applications to problems involving heights and distance
  - Get basic ideas of two dimensional geometry and graphing straight lines
  - Use various methods to compute the probabilities of events
  - Acquires basic ideas of derivatives, standard results and various rules for finding the derivatives of functions
  - Differentiate integration from differentiation and integration of simple functions
  - Acquires the basic arithmetic skills involving percentages, averages, time and rates, elementary algebra and geometry

SIXTH SEMESTER

### **MM6CRT09: REAL ANALYSIS**

After the completion of this course the student will be able to:

- Applies this term into problems ·
- Illustrate the convergence properties of power series
- Identifies Continuity and Discontinuity of various functions in different contexts
- Distinguish Uniform continuity from continuity and related theorems
- Understand Integrability and theorems on integrability
- Recognize the difference between pointwise and uniform convergence of a sequence of functions
- Illustrate the effect of uniform convergence on the limit function with respect to continuity, differentiability, and integrability

- Develops a knowledge about Riemann Integration and applies into problems
- Determine the Riemann integrability and the Riemann
- Apply the Mean Value Theorem and L'Hospital rules to problems in the context of real analysis

### **MM6CRT11: COMPLEX ANALYSIS**

On completion of this course, the students will be able to

- Compute sums, products, quotients, conjugate, modulus, and argument of complex numbers
- Define and analyze limits and continuity for complex functions as well as consequences of continuity
- Conceive the concepts of analytic functions and will be familiar with the elementary complex functions and their properties
- Determine whether a given function is differentiable, and if so find its derivative
- Use differentiation rules to compute derivatives
- Write complex numbers in polar form
- Evaluate exponentials and integral powers of complex numbers
- Find all integral roots and all logarithms of nonzero complex numbers
- Apply the concept and consequences of analyticity and the Cauchy-Riemann equations and of results on harmonic and entire functions including the fundamental theorem of algebra
- Find parameterizations of curves, and compute complex line integrals directly
- Understand the theory and techniques of complex integration
- Applies the theory into application of the power series expansion of analytic functions
- Understand the basic methods of complex integration and its application in contour integration.
- Analyze sequences and series of analytic functions and types of convergence,
- Evaluate complex contour integrals directly and by the fundamental theorem, apply the Cauchy integral theorem in its various versions, and the Cauchy integral formula
- Represent functions as Taylor, power and Laurent series, classify singularities and poles, find residues and evaluate complex integrals using the residue theorem
- Use the Cauchy Residue Theorem to evaluate integrals and sum series
- Identify the isolated singularities of a function and determine whether they are removable, poles, or essential
- Compute Laurent series at an isolated singularity, and determine the residue
- Understand uses of improper integrals in various situations
- Use the residue theorem to compute complex line integrals and real integrals

### **MM6CRT10: GRAPH THEORY AND METRIC SPACES**

After the completion of this course the student will be able to

- Understand the new topics Graph Theory
- Understand the basic concepts of graphs, directed graphs, and weighted graphs and able to present a graph by matrices
- Understand the properties of trees and able to find a minimal spanning tree for a given weighted graph
- Understand Eulerian and Hamiltonian graphs
- Recall the defining properties of a metric space, and determine whether a given function defines a metric
- Determine how that a function is or is not a metric
- Show that a set in a metric space is or is not open and/or closed
- Show that a function between metric spaces is or is not continuous
- Show that a sequence in a metric space is or is not convergent
- Show that a metric space is or is not complete
- Familiarize with open sets, closed sets and Cantor set

### **MM6CRT12: LINEAR ALGEBRA**

Upon completion of this course, students should be able to:

- Basic concepts and properties of Matrices
  - Understand the idea about vector space
  - Analyze finite and infinite dimensional vector spaces and subspaces over a field and their properties, including the basis structure of vector spaces
  - Use the definition and properties of linear transformations and matrices of linear transformations and change of basis, including kernel, range and isomorphism
  - Compute with the characteristic polynomial, eigenvectors, eigenvalues and Eigen spaces, as well as the geometric and the algebraic multiplicities of an eigen value and apply the basic diagonalization result

### **MM6PRT01 : Project**

- Demonstrate library research skills in the area of mathematics,
- Critique mathematical presentations, and
- Produce a mature oral presentation of a non-trivial mathematical topic.